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# Refinement of the Structure of Descloizite 

By F. C. Hawthorne<br>Department of Earth Sciences, University of Manitoba, Winnipeg, Manitoba R3T 2N2, Canada

and R. FagGiani<br>Materials Research Institute, McMaster University, Hamilton, Ontario L8S 4M1, Canada

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#### Abstract

PbZnVO}_{4} \mathrm{OH}\), orthorhombic, $\mathrm{Pnma}, \mathrm{Z}=4$, $D_{c}=6.202 \mathrm{Mg} \mathrm{m}^{-3}$; cell constants at $293 \mathrm{~K}: a=$ 7.593 (2), $b=6.057$ (1), $c=9.416$ (2) $\AA ; \lambda($ Мо K $)=$ $0.71069 \AA$. Examination of $41\left(\mathrm{VO}_{4}\right)$ tetrahedra in 31 crystal structures showed that the $\langle\mathrm{V}-\mathrm{O}\rangle$ bond length is significantly correlated with anion coordination number and the average electronegativity of the nextnearest neighbour cations, but not with tetrahedral distortion.


Introduction. Single-crystal precession photographs exhibited orthorhombic symmetry with systematic absences $h k 0, h=2 n+1 ; 0 k l, k+l=2 n+1, h 00$, $h=2 n+1 ; 0 k 0, k=2 n+1 ; 00 l, l=2 n+1$ consistent with the space group Pnma as assigned by Barnes \& Qurashi (1952). This was confirmed by the diffractometer data; none of the 0 kl reflexions listed by Qurashi \& Barnes (1964) as observed were greater than $2 \sigma$ above background. Perhaps these were due to Renninger effects in the earlier studies. Cell dimensions were determined by least-squares refinement of 15 reflexions automatically aligned on a four-circle diffractometer. Data collection and reduction procedures were as described by Hawthorne \& Calvo (1977); the crystal used for the data collection was ground to a sphere 0.14 mm in diameter. A total of 511 unique reflections were collected, of which 405 were considered as observed [ $I$ (net) $\geq 3 \sigma$ ]. Scattering factors for neutral atoms were taken from Cromer \& Mann (1968) with anomalous-dispersion corrections from Cromer \& Liberman (1970). Atomic parameters given by Qurashi \& Barnes (1954) were used as input to the leastsquares program RFINE (Finger, 1969), and with anisotropic thermal parameters of the form $\exp \left(-\sum_{i=1}^{3} \sum_{j=1}^{3} h_{i} h_{j} \beta_{i j}\right)$, convergence occurred at $R$ and $R_{w}$ factors (unit weights) of 4.9 and $5.8 \%$ respectively (observed reflections). Final parameters are given

in Table 1. Interatomic distances and angles were calculated with the program $\operatorname{ERRORS}$ (L. W. Finger, personal communication) and are given in Table 2.*

Discussion. It has been shown that mean interatomic distances in tetrahedral oxyanions are to some extent a function of the structure in which they occur. Shannon \& Prewitt (1969) and Brown \& Gibbs (1969) showed the effect of anion coordination number on $\langle\mathrm{Si}-\mathrm{O}\rangle$ distances, and Shannon (1971, 1975, 1976) and Shannon \& Calvo (1973a) have shown the effect of both anion coordination number and average cation electronegativity on mean bond lengths in numerous tetrahedral oxyanions. Baur (1974) showed that $\langle\mathrm{P}-\mathrm{O}\rangle$ distances are significantly affected by both anion coordination and tetrahedral distortion, and Brown \& Shannon (1973) have shown that distortion has a significant effect on mean bond lengths for octahedrally coordinated cations. One may thus conjecture

[^0]Table 2．Selected interatomic distances $(\AA)$ and angles $\left(^{\circ}\right)$ in descloizite

| $\mathrm{V}-\mathrm{O}(1)$ | $1.738(14) \times 2$ | $\mathrm{Pb}-\mathrm{O}(1)^{6}$ | 2.451 （17）$\times 2$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{V}-\mathrm{O}(2)^{a}$ | 1.645 （24） | $\mathrm{Pb}-\mathrm{O}(1)^{\text {d }}$ | 2.730 （15）$\times 2$ |
| $\mathrm{V}-\mathrm{O}(3)$ | 1.760 （23） | $\mathrm{Pb}-\mathrm{O}(2)^{e}$ | 2.790 （25） |
| ＜V－O ${ }^{\text {－}}$ | 1.720 | $\mathrm{Pb}-\mathrm{O}(3)^{r}$ | $2 \cdot 693$（22） |
|  |  | $\mathrm{Pb}-\mathrm{OH}^{8}$ | 2.443 （22） |
| $\mathrm{Zn}-\mathrm{O}(1)^{\text {b }}$ | 2.204 （14）$\times 2$ | $\langle\mathrm{Pb}-\mathrm{O}$ 〉 | 2.613 |
| $\mathrm{Zn}-\mathrm{O}(3)^{\text {c }}$ | $2 \cdot 182(16) \times 2$ |  |  |
| $\mathrm{Zn}-\mathrm{OH}$ | 1.973 （16）$\times 2$ |  |  |
| $\langle\mathrm{Zn}-\mathrm{O}\rangle$ | 2．120 |  |  |
| V tetrahedron |  |  |  |
| $\mathrm{O}(1)-\mathrm{O}(1)^{h}$ | 2.90 （3） | $\mathrm{O}(1)-\mathrm{V}(1)-\mathrm{O}(1)^{h}$ | 113.0 （9） |
| $\mathrm{O}(1)-\mathrm{O}(2)^{\text {a }}$ | 2.73 （3）$\times 2$ | $\mathrm{O}(1)-\mathrm{V}(1)-\mathrm{O}(2)^{a}$ | $107.8(7) \times 2$ |
| $\mathrm{O}(1)-\mathrm{O}(3)$ | 2.89 （2）$\times 2$ | $\mathrm{O}(1)-\mathrm{V}(1)-\mathrm{O}(3)$ | $111.6(6) \times 2$ |
| $\mathrm{O}(2)^{a}-\mathrm{O}(3)$ | 2.70 （3） | $\mathrm{O}(2)^{a}-\mathrm{V}(1)-\mathrm{O}(3)$ | 104.7 （10） |
| 〈O－O〉 | 2.81 | 〈O－V－O） | 109.4 |
| Zn octahedron |  |  |  |
| $\mathrm{O}(1)^{\text {b }}-\mathrm{O}(3)^{\text {c }}$ | $3 \cdot 10$（3）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Zn}-\mathrm{O}(3)^{c}$ | $90 \cdot 0$（7）$\times 2$ |
| $\mathrm{O}(1)^{b}-\mathrm{O}(3)^{f}$ | $3 \cdot 10$（2）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Zn}-\mathrm{O}(3)^{r}$ | 90.0 （7）$\times 2$ |
| $\mathrm{O}(1)^{b}-\mathrm{OH}$ | 2.95 （3）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Zn}-\mathrm{OH}$ | 89.5 （8）$\times 2$ |
| $\mathrm{O}(1)^{b}-\mathrm{OH}^{l}$ | 2.97 （2）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Zn}-\mathrm{OH}^{t}$ | 90.5 （8）$\times 2$ |
| $\mathrm{O}(3)^{\mathrm{c}}-\mathrm{OH}$ | 3.05 （3）$\times 2$ | $\mathrm{O}(3)^{c}-\mathrm{Zn}-\mathrm{OH}$ | 94.2 （7）$\times 2$ |
| $\mathrm{O}(3)^{c}-\mathrm{OH}^{\text {d }}$ | 2.83 （3）$\times 2$ | $\mathrm{O}(3)^{c}-\mathrm{Zn}-\mathrm{OH}^{l}$ | $85.8(7) \times 2$ |
| ＜O－O〉 | 3.00 | $\langle\mathrm{O}-\mathrm{Zn}-\mathrm{O}\rangle$ | 90.0 |
| Pb polyhedron |  |  |  |
| $\mathrm{O}(1)^{b}-\mathrm{O}(1)^{\text {d }}$ | 5.00 （2）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Pb}-\mathrm{O}(1)^{d}$ | 149.3 （1）$\times 2$ |
| $\mathrm{O}(1)^{b}-\mathrm{O}(1)^{i}$ | 3．16（3） | $\mathrm{O}(1)^{b}-\mathrm{Pb}-\mathrm{O}(1)^{i}$ | 80.2 （7） |
| $\mathrm{O}(1)^{0}-\mathrm{O}(1)^{j}$ | 3.87 （2）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Pb}-\mathrm{O}(1)^{j}$ | 96.5 （4）$\times 2$ |
| $\mathrm{O}(1)^{b}-\mathrm{O}(2)^{e}$ | 4.49 （2）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Pb}-\mathrm{O}(2)^{e}$ | $117.9(5) \times 2$ |
| $\mathrm{O}(1)^{b}-\mathrm{O}(3)^{f}$ | $3 \cdot 10$（3）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Pb}-\mathrm{O}(3)^{f}$ | $74.0(5) \times 2$ |
| $\mathrm{O}(1)^{b}-\mathrm{OH}^{8}$ | $3 \cdot 15$（2）$\times 2$ | $\mathrm{O}(1)^{b}-\mathrm{Pb}-\mathrm{OH}^{8}$ | $80 \cdot 2(6) \times 2$ |
| $\mathrm{O}(1)^{d}-\mathrm{O}(1)^{j}$ | $3 \cdot 16$（3） | $\mathrm{O}(1)^{d}-\mathrm{Pb}-\mathrm{O}(1)^{j}$ | 70.7 （7） |
| $\mathrm{O}(1)^{d}-\mathrm{O}(2)^{e}$ | 3.93 （3）$\times 2$ | $\mathrm{O}(1)^{d}-\mathrm{Pb}-\mathrm{O}(2)^{e}$ | $90.8(5) \times 2$ |
| $\mathrm{O}(1)^{d}-\mathrm{O}(3)^{f}$ | 5.01 （3）$\times 2$ | $\mathrm{O}(1)^{d}-\mathrm{Pb}-\mathrm{O}(3)^{f}$ | $134.9(4) \times 2$ |
| $\mathrm{O}(1)^{d}-\mathrm{OH}^{8}$ | 2.95 （3）$\times 2$ | $\mathrm{O}(1)^{d}-\mathrm{Pb}-\mathrm{OH}^{8}$ | 69.2 （6）$\times 2$ |
| $\mathrm{O}(2)^{e}-\mathrm{O}(3)^{f}$ | 2.70 （3） | $\mathrm{O}(2)^{e}-\mathrm{Pb}-\mathrm{O}(3)^{f}$ | 58.9 （6） |
| $\mathrm{O}(2)^{e}-\mathrm{OH}^{8}$ | $5 \cdot 11$（3） | $\mathrm{O}(2)^{e}-\mathrm{Pb}-\mathrm{OH}^{8}$ | 155.1 （8） |
| $\mathrm{O}(3)-\mathrm{OH}^{8}$ | 4.91 （3） | $\mathrm{O}(3)^{f-\mathrm{Pb}}-\mathrm{OH}^{8}$ | 146.0 （8） |

Symmetry code：$(a)=1+x, y, z ;(b)=x-\frac{1}{2}, \frac{1}{2}-y, z ;(c)=x$ ， $y-1, z ;(d)=x-1, y, z ;(e)=-x, 1-y,-z ;(f)=1-x, 1-y$ ， $-z ;(g)=x-\frac{1}{2}, y, \frac{1}{2}-z ;(h)=x, 1 \frac{1}{2}-y, z ;(i)=x-\frac{1}{2}, y, z ;$ $(j)=x-1, \frac{1}{2}-y, z ;(k)=1 \frac{1}{2}-x, y-\frac{1}{2},-z ;(l)=1-x,-y,-z$ ．
that mean interatomic distances in tetrahedral oxy－ anions are a function of anion coordination number， average cation electronegativity and tetrahedral distor－ tion．Baur（1978）has examined the effect of these three variables，together with several others，on $\langle\mathrm{Si}-\mathrm{O}\rangle$ bond lengths，and has shown that only anion coordination number，the number of bridging anions per tetrahedron and the mean value of the secant of the bridging angles $\mathrm{Si}-\mathrm{O}-T$ contribute significantly to $\langle\mathrm{Si}-\mathrm{O}\rangle$ variations． Variation in bridging angles $\mathrm{V}-\mathrm{O}-T$ was not con－ sidered in the present study as we are interested in the development of an equation for predictive purposes in the simulation of crystal structures．

A total of $41\langle\mathrm{~V}-\mathrm{O}\rangle$ distances（Table 3）were used，
data being included only if $\langle\sigma\rangle \leq 0.01 \AA$ ．Data for $\mathrm{Ca}_{3} \mathrm{~V}_{2} \mathrm{O}_{8}$（Gopal \＆Calvo，1973a）were excluded because the presence of positional disorder has affected the observed V－O distances．Anion coordination numbers（ CN ）were evaluated individually，the parameter $\Delta$（Brown \＆Shannon，1973）was used as a measure of tetrahedral distortion and the tetrahedral angle variance $\lambda$（Robinson，Gibbs \＆Ribbe，1971）was evaluated．The electronegativity was also evaluated in－ dividually，as the average electronegativity per cation－ -O bond $\left\{\bar{\chi}=\left[\left(\sum_{\mathrm{CN}} \chi^{\mathrm{cat}}\right)-\chi^{\mathrm{V}}\right] /(\mathrm{CN}-1)\right\}$ ．The grand $\langle\mathrm{V}-\mathrm{O}\rangle^{1 \mathrm{~V}}$ distance is 1.721 （8）$\AA$ ．The tetra－ hedral angle variance and the number of bridging anions per tetrahedron did not show significant correlation with either $\langle\mathrm{V}-\mathrm{O}\rangle$ or the mean ionic radius of $\mathrm{V}^{5+}$ and are not considered further．A stepwise linear regression was performed on $\langle\mathrm{V}-\mathrm{O}\rangle, \Delta, \mathrm{CN}$ and $\bar{\chi}$ with $\langle\mathrm{V}-\mathrm{O}\rangle$ as the dependent variable．The correlation with CN was not significant at the 0.01 level．Baur（1974） has argued that the variation in ionic radii for $\mathrm{O}^{2-}$ given by Shannon \＆Prewitt（1969）is a good measure of the variation in $\langle X-\mathrm{O}\rangle$ bond lengths due to variation in anion coordination number．Accepting this，the effect of anion coordination number may be removed by using ionic radius instead of $\langle\mathrm{V}-\mathrm{O}\rangle$ distance．Stepwise linear regression was performed on $r^{v}, \Delta$ and $\bar{\chi}$ with $r^{v}$ as the dependent variable；the correlation with $\Delta$ was not significant at the 0.01 level．Hence the ionic radius of $\mathrm{V}^{5+}$ in tetrahedral coordination appears to be solely a function of the electronegativity of the next－nearest neighbour cations：

$$
r\left(\mathrm{~V}^{5+}\right)=0.325+0.020(3) \bar{\chi}, \quad R=0.724
$$

This may be incorporated with the dependence of $r\left(\mathrm{O}^{2-}\right)$ on coordination number to give the equation

$$
\langle\mathrm{V}-\mathrm{O}\rangle=1.649+0.020 \bar{\chi}+0.013 \mathrm{CN} .
$$



Fig．1．Comparison of observed and calculated $\langle\mathrm{V}-\mathrm{O}\rangle$ distances．

Table 3. Data for vanadate structures
$\bar{\chi}=\left(\sum_{\mathrm{cN}} \chi^{\text {cat }}-\chi^{\mathrm{v}}\right) /(\mathrm{CN}-1) ; \Delta=\sum_{i=1}^{4}\left[\left(l_{i}-\langle l\rangle\right) /\langle I\rangle\right]^{2} \times 10^{3} / 4$.

|  | $\langle\mathrm{V}-\mathrm{O}\rangle_{o}(\AA)$ | CN | $r(\AA)$ | $\bar{\chi}$ | $\Delta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Pb}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{\text {a }}$ | 1.721 (6) | 3.25 | 0.355 | 1.90 | 1.04 |
|  | 1.726 (5) | $3 \cdot 50$ | 0.357 | 1.90 | 1.11 |
| $\mathrm{LiVO}_{3}{ }^{\text {b }}$ | 1.727 (1) | $3 \cdot 25$ | 0.361 | 1.20 | $2 \cdot 30$ |
| $\mathrm{Cu}_{5} \mathrm{~V}_{2} \mathrm{O}_{10}{ }^{\text {c }}$ | 1.722 (2) | $3 \cdot 25$ | 0.356 | 2.00 | 0.54 |
|  | 1.725 (2) | $3 \cdot 50$ | 0.356 | 2.00 | 0.75 |
| $\mathrm{Mg}_{3} \mathrm{~V}_{2} \mathrm{O}_{8}{ }^{\text {d }}$ | 1.729 (1) | 3.25 | 0.363 | 1.20 | 0.78 |
| $\mathrm{Cu}_{3} \mathrm{~V}_{2} \mathrm{O}_{8}{ }^{\text {e }}$ | 1.726 (2) | 3.25 | 0.360 | 2.00 | 0.75 |
| $\mathrm{Zn}_{3} \mathrm{~V}_{2} \mathrm{O}_{8}{ }^{\text {f }}$ | 1.715 (5) | 3.25 | 0.349 | 1.60 | 0.84 |
| $\mathrm{Ba}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{8}$ | 1.715 (3) | 3.50 | 0.346 | 1.00 | 1.24 |
|  | 1.721 (3) | 3.74 | 0.348 | 0.99 | 1.25 |
|  | 1.715 (3) | 3.50 | 0.346 | 1.00 | 1.19 |
|  | 1.724 (3) | 3.50 | 0.355 | 1.00 | 1.35 |
| $\mathrm{Zn}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{\text {n }}$ | 1.716 (3) | 2.50 | 0.359 | 1.65 | 0.61 |
| $\mathrm{Co}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{\text {a }}$ | 1.732 (2) | 2.75 | 0.372 | 1.82 | 2.01 |
|  | 1.734 (2) | 3.00 | 0.371 | 1.82 | 1.31 |
| $\mathrm{Ni}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{\text {i }}$ | 1.728 (2) | 2.75 | 0.368 | 1.90 | 2.02 |
|  | 1.732 (2) | 3.00 | 0.369 | 1.90 | 1.29 |
| $\mathrm{Li}_{3} \mathrm{VO}_{4}{ }^{j}$ | 1.717 (1) | 4.00 | 0.341 | 1.00 | 0.00 |
| $\mathrm{Co}_{3} \mathrm{~V}_{2} \mathrm{O}_{8}{ }^{\text {k }}$ | 1.732 (3) | $3 \cdot 25$ | 0.366 | 1.80 | 0.68 |
| $\mathrm{Ni}_{3} \mathrm{~V}_{2} \mathrm{O}_{8}{ }^{k}$ | 1.736 (1) | $3 \cdot 25$ | 0.370 | 1.90 | 0.68 |
| $\mathrm{NdVO}_{4}{ }^{\text {d }}$ | 1.721 (5) | 3.00 | 0.358 | 1.20 | 0.00 |
| $\mathrm{YVO}_{4}{ }^{\text {m }}$ | 1.718 (2) | 3.00 | 0.355 | 1.20 | 0.00 |
| FeVO ${ }_{4}{ }^{\text {n }}$ | 1.720 (4) | 2.50 | 0.363 | 1.90 | 1.40 |
|  | 1.727 (4) | $2 \cdot 50$ | 0.370 | 1.90 | 1.07 |
|  | 1.720 (4) | 2.25 | $0 \cdot 367$ | 1.90 | 0.91 |
| $\mathrm{Ca}_{2} \mathrm{VO}_{4} \mathrm{Cl}^{\circ}$ | 1.707 (1) | 4.00 | 0.331 | 1.00 | 0.01 |
| $\mathrm{Cd}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{\text {p }}$ | 1.718 (10) | 2.75 | 0.358 | 1.73 | 0.36 |
| $\mathrm{Ca}_{5}\left(\mathrm{VO}_{4}\right)_{3} \mathrm{OH}^{\text {q }}$ | 1.707 (2) | 4.00 | 0.331 | 1.00 | 0.06 |
| $\mathrm{NaVO}_{3}{ }^{\text {r }}$ | 1.723 (1) | $3 \cdot 25$ | 0.357 | 1.12 | $2 \cdot 20$ |
| $\mathrm{KVO}_{3}{ }^{5}$ | 1.724 (2) | $4 \cdot 50$ | 0.342 | 0.84 | $2 \cdot 29$ |
| $\mathrm{RbVO}_{3}{ }^{\text {s }}$ | 1.717 (3) | 4.50 | 0.335 | 0.84 | $2 \cdot 50$ |
| $\mathrm{CsVO}_{3}{ }^{\text {s }}$ | 1.721 (3) | 4.50 | 0.339 | 0.77 | 2.40 |
| $a-\mathrm{Cu}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{\text {a }}$ | 1.709 (2) | 2.50 | 0.352 | 1.99 | 0.48 |
| $\beta-\mathrm{Cu}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{4}$ | 1.712 (3) | 2.50 | 0.355 | 1.49 | 0.78 |
| $\alpha-\mathrm{Na}_{3} \mathrm{Er}\left(\mathrm{VO}_{4}\right)_{2}{ }^{\text {v }}$ | 1.708 (2) | 3.75 | 0.335 | 0.98 | 0.41 |
| $\mathrm{Mg}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}{ }^{\mathbf{w}}{ }^{\text {a }}$ | 1.715 (2) | 2.75 | 0.355 | 1.82 | 1.53 |
|  | 1.729 (2) | 3.00 | 0.366 | 1.74 | 0.50 |
| $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{O}_{8}{ }^{\text {a }}$ | 1.705 (3) | 4.00 | 0.329 | 0.90 | 1.20 |
| $\mathrm{Ca}_{2} \mathrm{~V}_{2} \mathrm{O}_{7} \cdot \mathrm{H}_{2} \mathrm{O}^{y}$ | 1.719 (4) | 3.00 | 0.356 | $1 \cdot 12$ | 0.77 |
|  | 1.716 (4) | 3.00 | 0.359 | 1.12 | 0.94 |
| $\mathrm{PbZnVO} 4 \mathrm{OH}^{2}$ | 1.720 (9) | $3 \cdot 50$ | 0.351 | 1.78 | 0.67 |

References: (a) Shannon \& Calvo (1973b). (b) Shannon \& Calvo (1973c). (c) Shannon \& Calvo (1973d). (d) Krishnamachari \& Calvo (1971). (e) Shannon \& Calvo (1972). ( $f$ ) Gopal \& Calvo (1971). (g) Hawthorne \& Calvo (1978). (h) Gopal \& Calvo (1973b). (i) Sauerbrei, Faggiani \& Calvo (1974). (j) Shannon \& Calvo (1973a). (k) Sauerbrei, Faggiani \& Calvo (1973). (l) Baglio \& Sovers (1971). ( $m$ ) Lohmüller, Schmidt, Deppisch, Gramlich \& Scheringer (1973). ( $n$ ) Robertson \& Kostiner (1972). (o) Banks, Greenblatt \& Post (1970). (p) Au \& Calvo (1967). (q) Kutoglu (1974). (r) Marumo, Isobe \& Iwai (1974). (s) Hawthorne \& Calvo (1977). (t) Calvo \& Faggiani (1975). (u) Mercurio-Lavaud \& Frit (1973). (v) Salmon, Parent, Le Flem \& Vlasse (1976). (w) Gopal \& Calvo (1974). (x) Galy \& Carpy (1975). (y) Konnert \& Evans (1975). (z) This work.

A number of observed and calculated $\langle\mathrm{V}-\mathrm{O}\rangle$ distances using this equation are given in Fig. 1. These equations should be of use both for predictive purposes and as a check on observed $\left\langle\mathrm{V}^{\mathrm{S}+}-\mathrm{O}\right\rangle^{\text {IV }}$ distances.

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# Paradamite 

By F. C. Hawthorne<br>Department of Earth Sciences, University of Manitoba, Winnipeg, Manitoba R3T 2N2, Canada

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#### Abstract

Zn}_{2} \mathrm{AsO}_{4} \mathrm{OH}, P \overline{1}, Z=2, D_{c}=4.595 \mathrm{Mg}\) $\mathrm{m}^{-3}$; cell constants at $293 \mathrm{~K}: a=5.638(3), b=$ 5.827 (3), $c=6.692$ (2) $\AA, \alpha=103.25$ (4), $\beta=$ 104.37 (3), $\gamma=87.72$ (4) ${ }^{\circ} ; \lambda($ Мо $K \alpha)=0.71069 \AA$.


 Paradamite is isostructural with tarbuttite, $\mathrm{Zn}_{2} \mathrm{PO}_{4} \mathrm{OH}$.Introduction. Paradamite is a dimorph of adamite and was first characterized by Switzer (1956). Finney (1966) derived the unit cell and proposed that paradamite is isostructural with tarbuttite, $\mathrm{Zn}_{2} \mathrm{PO}_{4} \mathrm{OH}$, and Hawthorne (1976) has discussed the relationship between the adamite and tarbuttite structure types.

Single-crystal precession photographs of paradamite from Mapimi, Mexico, exhibit triclinic symmetry; the unit cell chosen is analogous to that used by Cocco, Fanfani \& Zanazzi (1966) for tarbuttite. The unit-cell parameters were derived by least-squares refinement of 15 high-angle reflexions aligned automatically on a four-circle diffractometer. A full set of intensity data ( 1384 reflexions) was collected over one hemisphere out to a $2 \theta$ of $65^{\circ}$ from an irregular equidimensional crystal of radius 0.09 mm , following the experimental procedure of Hawthorne \& Ferguson (1975). Standard data-reduction procedures with a spherical absorption correction ( $\mu=20.2 \mathrm{~mm}^{-1}$ ) resulted in 1202 unique reflexions of which 1132 were considered as observed ( $I_{\text {net }}>3 \sigma$ ). Structure refinement was carried out on an IBM 370/158 computer using the program RFINE
(Finger, 1969). Scattering factors for neutral atoms were taken from Cromer \& Mann (1968) with anomalous-dispersion corrections from Cromer \& Liberman (1970). The atomic parameters given by Cocco et al. (1966) for tarbuttite, $\mathrm{Zn}_{2} \mathrm{PO}_{4} \mathrm{OH}$, were assumed as the starting parameters for paradamite. Several cycles of full-matrix least-squares refinement resulted in convergence (for isotropic temperature factors) at a conventional $R$ of $6 \cdot 2 \%$ (observed reflexions). Conversion to anisotropic temperature factors of the form $\exp \left(-\sum_{i=1}^{3} \sum_{j=1}^{3} h_{i} h_{j} \beta_{i j}\right)$ resulted in convergence (maximum shift/error $<0.01$ ) at an $R$ of $4.8 \%$ and an $R_{w}$ (unit weights) of $5.8 \%$. Final atomic positions and equivalent isotropic temperature factors are given in Table 1. Interatomic distances and angles

Table 1. Atomic positions and equivalent isotropic temperature factors ( $\AA^{2}$ )

|  | $x$ | $y$ | $z$ | $B_{\text {ea }}$ |
| :--- | :--- | :--- | :--- | :--- |
|  | $\boldsymbol{c}$ |  |  |  |
| $\mathrm{Zn}(1)$ | $0.3928(2)$ | $0.2498(2)$ | $0.5008(2)$ | $0.86(2)$ |
| $\mathrm{Zn}(2)$ | $0.0214(2)$ | $0.7355(2)$ | $0.1867(1)$ | $0.72(2)$ |
| As | $0.8312(2)$ | $0.2476(1)$ | $0.2745(1)$ | $0.49(2)$ |
| $\mathrm{O}(1)$ | $0.7627(11)$ | $0.9689(0)$ | $0.1391(9)$ | $0.79(9)$ |
| $\mathrm{O}(2)$ | $0.9421(12)$ | $0.3885(11)$ | $0.1233(9)$ | $0.94(9)$ |
| $\mathrm{O}(3)$ | $0.5779(11)$ | $0.3837(11)$ | $0.3342(9)$ | $0.85(9)$ |
| $\mathrm{O}(4)$ | $0.9549(11)$ | $0.7478(11)$ | $0.4968(9)$ | $0.71(8)$ |
| OH | $0.3519(11)$ | $0.8899(12)$ | $0.2997(9)$ | $0.89(9)$ |

[^1]
[^0]:    * Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34060 ( 4 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH 1 2HU, England.

[^1]:    C 1979 International Union of Crystallography

